A LEVEL 2 MODULE, SPRING SEMESTER 2021-2022

THERMODYNAMICS AND FLUID MECHANICS 2

SOLUTIONS

MMME2047-E1

END

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- 1. A solid biomass has an ultimate gravimmetric composition of 48% carbon, 6% hydrogen and 44% oxygen. It is burned completely in air in a power generation plant, and produces an exhaust stream with 5% oxygen in the wet products by volume.
 - (a) Determine the mass and number of moles of carbon dioxide and water vapour produced by the stoichiometric combustion of 1 kg of the biomass.

.. for 0.48 kg C, 44 x0.48 = 1.76 kg [1] $M_{1} = 22 + 44$ Nº. of Moler of CO2 per by fuel [1] <u>1.76 kg</u> = 0.040 knest 44 kg/knost = 40 moter for 0.06 kg H, 18x 0.06 = 0.54 kg[1] $\begin{array}{c} H_2 + \frac{1}{2}O_2 \rightarrow H_2O\\ \widetilde{M}_i \quad 2 \quad 16 \quad 18 \end{array}$ Nº of rister of H20 per by fiel $\frac{0.54}{18} = 0.03 \text{ kmol}$ = 30 mols [1]

in absence of correct form of responses, 1 mark for getting the molar masses(b) Calculate the mass of air required for stoichiometric combustion of 1 kg

of biomass.

[5]

[4]

fir delenvire amount of 02 required Man elloz - Manaf C: 1.76 - 0.48 = 1.28 kg 02 man al H20 - manof H = 0.54 - 0.06 = 0.48 kg 62 = 0.44 man of O in fuel ... mon of 02 required is: 1.28 + 6.48 - 0.44 = 1.32 kg 2 that is per by of fiel, and assuming the O in fiel is one to burn the C & H congonants. . man ob air requires, using the rate of air to O2: 4.29 kg air/kg 0 2 × 1.82 kg 02 > 5.66 kg au per kg Fuel. [3]

(c) Given that the volume fractions of the exhaust gases are N₂ 31.9%, O₂ 4.8%, CO₂ 36.2 %, H₂O 27.1%, use a table of the wet products of combustion to help determine the specific heat capacity at constant pressure for the product gas mixture at 300 K.

	0·05 = 15·	5+3.76	x + 4	0+30	4.275+ 6 >(- 6 26	
Table of	protects: 1 ri - 10 40 30 20		hg/ko	w[1]	m[]	[1] Mi-Nimi	[1]
component	li ric- 10 40	ni/n 0.362	m _i 44	Cpi 0.846	15.928	0.509	0.431
		, x	ιv				
0,	5 3762 35.30 5.26	0.048	32	0.918 m=1	1-536 E= 31.274	0-049 Sp =	0.045
G	riven –			k	g/km&1.		kJ/kgK

specific molar is acceptable using volume fractions, works out as 33 kJ/kmolK

(a) A single pass, counterflow shell and tube heat exchanger uses tubes of diameter 20 mm with water flowing at the rate of 0.1 kg/s in each tube at 20 °C. Calculate the heat transfer coefficient at the inner wall of the tube given the Nusselt number correlations:

 $Nu = 0.023 Re^{0.8} Pr^{0.4}$ For turbulent flow, and

[4]

half mark deducted on Re for using air or steam rather than water – full marks if method ok following

(c) The heat exchanger has a shell and tube arrangement, containing 10 tubes, with a flow of air entering the shell at 1000 K. The air enters at a flow rate of 0.5 kg/s and the heat transfer coefficient on the outer surface of the tubes is 100 W/m²K, and the conduction resistance of the pipe wall is negligible. Calculate the overall heat transfer coefficient and the length of the tubes in order to produce a gas exit temperature of 400 K. The correction factor may be assumed to be 1.0.

[8]

at least half marks for method if wrong values used

Q= Mair Cpair STair. Use c_{p} values lose bo (1000-273) Gair = $C_{p,800^{\circ}C} + C_{p,200^{\circ}C} = 1.1411 + 1.0185 = 1.07773[1]$ $= 727^{\circ}C,400$ will do for quickness 2 awd (400-278) = 127PC Q = 0.5 × 1.07773 × (727 - 127) = 3239 kW [1] U= L RTH A RTH = hAONT hAIN 94 W/M2K STM: STA-STR ler LSTA/K-[2] It The Cp is dependent on temperature, but this Gi pounded to 1 d.p. in is 10×09 kg/s: 10 tubes of water for 1 shell of air. Stw: 325 4.2x1 STM : $\frac{727 - 96}{\ln(727 - 20)} = 295 ^{\circ}C$ $\ln(727 - 96)$ [2] Q: UASTM : 323000 = 94 × (T×0.02 × L× 10) × 295 '17 -> L = 18.5M

3. A small airship, shown in Figure Q.1a, is cruising at a steady speed and constant altitude at a velocity of 20 km \cdot h⁻¹. It is filled entirely with 4000 m³ of helium. The temperature of the surrounding air is 286 K.

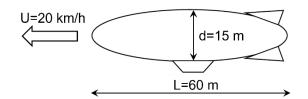


Figure Q.1a: Airship dimensions. The airship cross-section is circular.

(a) Calculate the Reynolds number of the airship based on diameter. Given the transition to turbulent flow occurs at $Re = 2 \times 10^5$, state whether the flow past the airship is turbulent or laminar. (Take the density of air to be 1.2 kg·m⁻³ and the kinematic viscosity to be 1.4×10^{-5} m²·s⁻¹). [2]

$$Re = \frac{Ud}{v} = \frac{5.55 \frac{m}{s} \times 15 m}{1.4 \times 10^{-5} \frac{m^2}{s}} = 5.94 \times 10^6$$

Therefore flow is turbulent. Marking scheme: [-1] for any mistake.

(b) The airship can be approximated by a three-dimensional ellipsoid. Using the information in Table Q.1b that shows C_D values as a function of L/d, estimate the drag coefficient of the airship, and calculate the drag force.



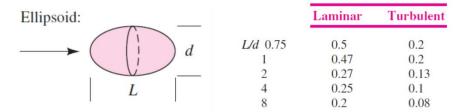


Figure Q.1b: Drag coefficients of an ellipsoid, based on frontal area.

L/d=4 and thus C_D=0.1 [2]. Frontal area: A=pi*D²/4=176.6 m²[2]. Drag force [1].

$$D = \frac{1}{2}C_D \rho U^2 A = \frac{1}{2} \times 0.1 \times 1.2 \frac{kg}{m^3} \times \left(5.55 \frac{m}{s}\right)^2 \times 176.6 m^2 = 326.4 N$$

(c) A problem develops with the airship and helium leaks through a nozzle to atmospheric pressure of 0.99 bar. By treating the flow through the system as one-dimensional isentropic, and neglecting all friction losses, calculate the Mach number of the helium at the nozzle if the stagnation pressure of helium in the airship is 1.2 bar. Take the ratio of specific

heats for Helium (g) to be 1.66 and the gas constant for helium, R_{helium} to be 2077 J·kg^-1·K^-1

$$\frac{p_0}{p} = \left[1 + Ma^2 \frac{\gamma - 1}{2}\right]^{\frac{\gamma}{\gamma - 1}} \Longrightarrow Ma^2 = \left[\left(\frac{p_0}{p}\right)^{\frac{\gamma - 1}{\gamma}} - 1\right] \frac{2}{\gamma - 1} = \left[\left(\frac{1.2 \ bar}{0.99 \ bar}\right)^{\frac{1.66 - 1}{1.66}} - 1\right] \frac{2}{1.66 - 1} = 0.241$$

Therefore, Ma=sqrt(0.241)=0.491 [3]

(d) Assuming the helium inside the airship has the same temperature as the surrounding air, what is the temperature of helium at the point of exit through the nozzle?

$$\frac{T_0}{T} = 1 + Ma^2 \frac{\gamma - 1}{2} = 1 + 0.491^2 \frac{1.66 - 1}{2} = 1.08$$

Therefore, since T₀=286 K, T=T₀/1.08=265.8 K [3]

- 4. A centrifugal pump is used to mobilise $Q=10 \text{ m}^3 \cdot \text{h}^{-1}$ of viscous oil, density $r=900 \text{ kg} \cdot \text{m}^{-3}$. The pump being used is the 4.75" pump from the HTO-80 series from MP Pumps Inc, the performance curves for the pump are shown in Figure Q.2.
 - (a) Using the graph and appropriate calculations, determine the head delivered by the pump, the differential pressure generated, the efficiency of the pump, the power delivered to the fluid and the brake horsepower in Watts, with the pump operating at 3450 rpm. Note that 1 hp=746 W.
 - From the graph in Fig. Q2, the 4.75" pump at a flow rate of $Q = 10 m^3/h$ generates a head of H = 21 m [1]. The differential pressure generated is [1]:

$$\Delta p = \rho g H = 900 \ \frac{kg}{m^3} \times 9.81 \frac{m}{s^2} \times 21 \ m = 185.4 \ kPa$$

From the graph, the pump efficiency is about $\eta = 0.51$ [1]. The power delivered to the fluid is [1]:

$$P_{w} = \rho g Q H = 900 \frac{kg}{m^{3}} * 9.81 \frac{m}{s^{2}} * 0.0028 \frac{m^{3}}{s} * 21 m = 519 W$$

- The pump input power [1] can either be calculated as $P = P_w / \eta = 1018 W$, or extracted from the graph obtaining P = 1.3 hp = 970 W. Is it also possible to extract the brake horsepower from the graph and then use the water horsepower evaluated above to calculate the efficiency, this would give a similar value $\eta = \frac{P_w}{p} = 0.535$.
- (b) If the eye of the pump has a diameter of D=5 cm, what should be the lowest oil pressure at the inlet to prevent cavitation? Consider that the vapour pressure of oil at the inlet is $p_v=15$ kPa.
- At $Q = 10 m^3/h$, the NPSH of the pump is about NPSH=3 m [1]. To avoid cavitation, it is necessary that [1]:

$$\frac{p_i}{\rho g} + \frac{v_i^2}{2g} - \frac{p_v}{\rho g} > NPSH \Longrightarrow p_i \ge \rho g \left(NPSH - \frac{v_i^2}{2g} + \frac{p_v}{\rho g} \right)$$

The velocity of the water at the inlet is [2]:

$$v_i = \frac{4Q}{\pi D_i^2} = \frac{4 * 0.0028 \frac{m^2}{s}}{\pi * (0.05 m)^2} = 1.43 \frac{m}{s}$$

....3

So that [1]:

$$p_i \ge 900 \frac{kg}{m^3} * 9.81 \frac{m}{s^2} * \left[3 m - \frac{\left(1.43 \frac{m}{s}\right)^2}{2 * 9.81 \frac{m}{s^2}} + \frac{15000 Pa}{900 \frac{kg}{m^3} * 9.81 \frac{m}{s^2}} \right] = 40525 Pa$$

(c) The company wish to operate at a higher flowrate of Q=19 m³·h⁻¹. The engineer considers buying a larger pump from the same series and operate at the same speed. Using pump similarity laws, work out what size pump should be bought and what power it will require. Using similarity rules [2]: [5]

[3]

[5]

$$\frac{Q_2}{Q_1} = \left(\frac{D_2}{D_1}\right)^3 \Longrightarrow D_2 = D_1 \left(\frac{Q_2}{Q_1}\right)^{\frac{1}{3}} = 4.75'' \times \left(\frac{19\,m^3/h}{10\,m^3/h}\right)^{\frac{1}{3}} = 5.9''$$

The power it will require [1]:

$$P_2 = P_1 \left(\frac{D_2}{D_1}\right)^5 = 1018 W \times \left(\frac{5.9''}{4.75''}\right)^5 = 3008 W$$

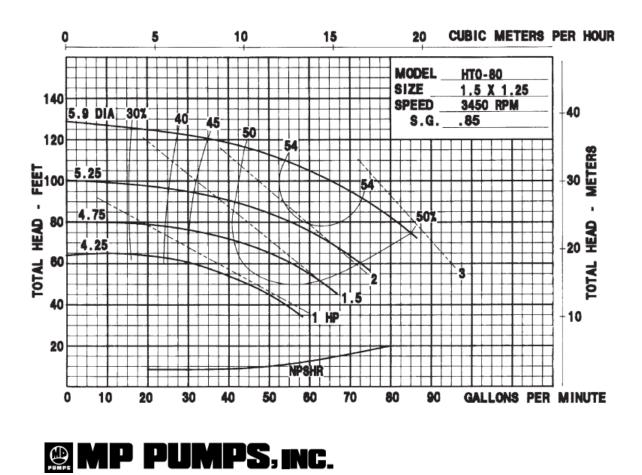


Figure Q.2: Performance curves for pump HTO-80.